

Description and testing of networks

Birgit Kriener

Computational Neuroscience Group, Ås, Norway



Why bother with the
description of network structure ?

Why bother with the description of network structure ?

- ▶ ensure reproducibility

Why bother with the description of network structure ?

- ▶ ensure reproducibility
- ▶ improve comparability to other network models and neuroanatomy

Why bother with the description of network structure ?

- ▶ ensure reproducibility
- ▶ improve comparability to other network models and neuroanatomy
- ▶ aid understanding of activity dynamics in complex networks

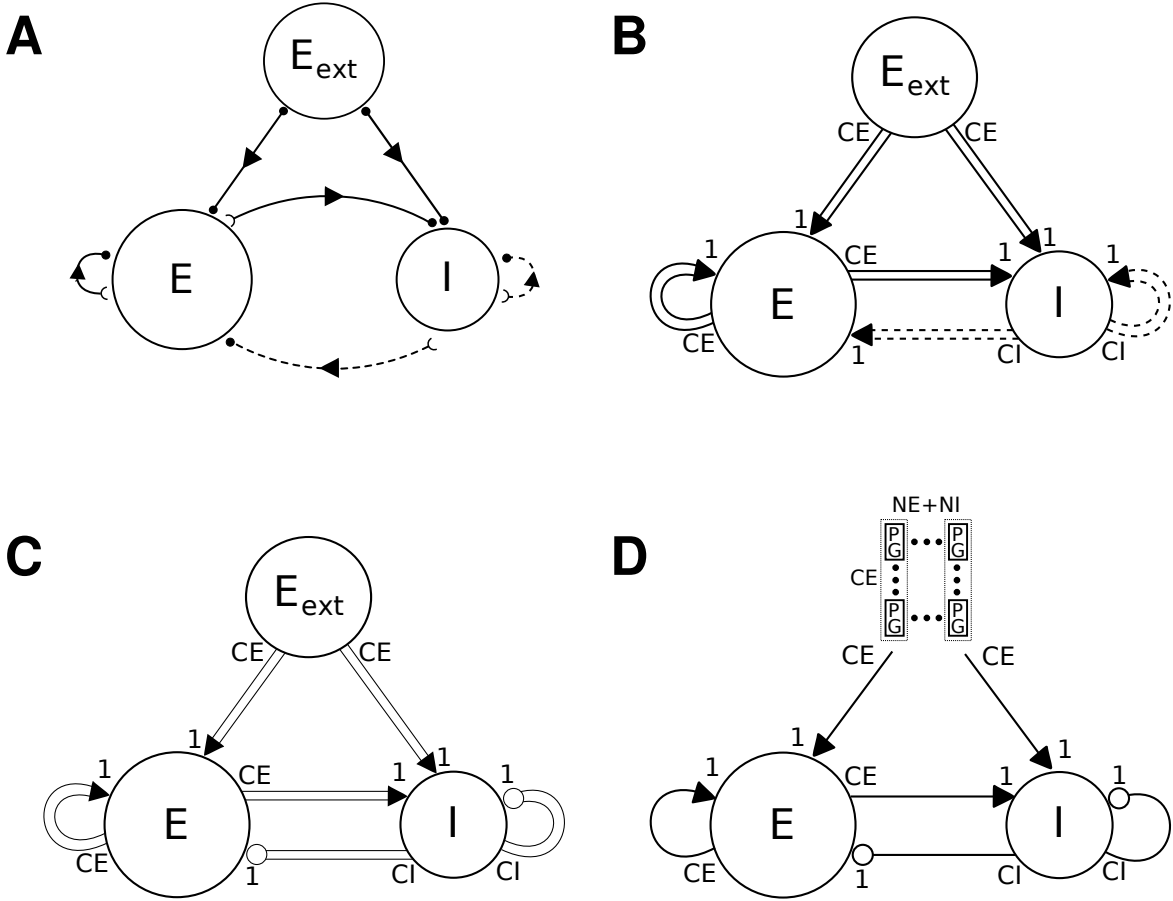
Why bother with the description of network structure ?

- ▶ ensure reproducibility
- ▶ improve comparability to other network models and neuroanatomy
- ▶ aid understanding of activity dynamics in complex networks
- ▶ facilitate optimal coding
- ▶ ...

Still lack of consensus of how to describe networks:

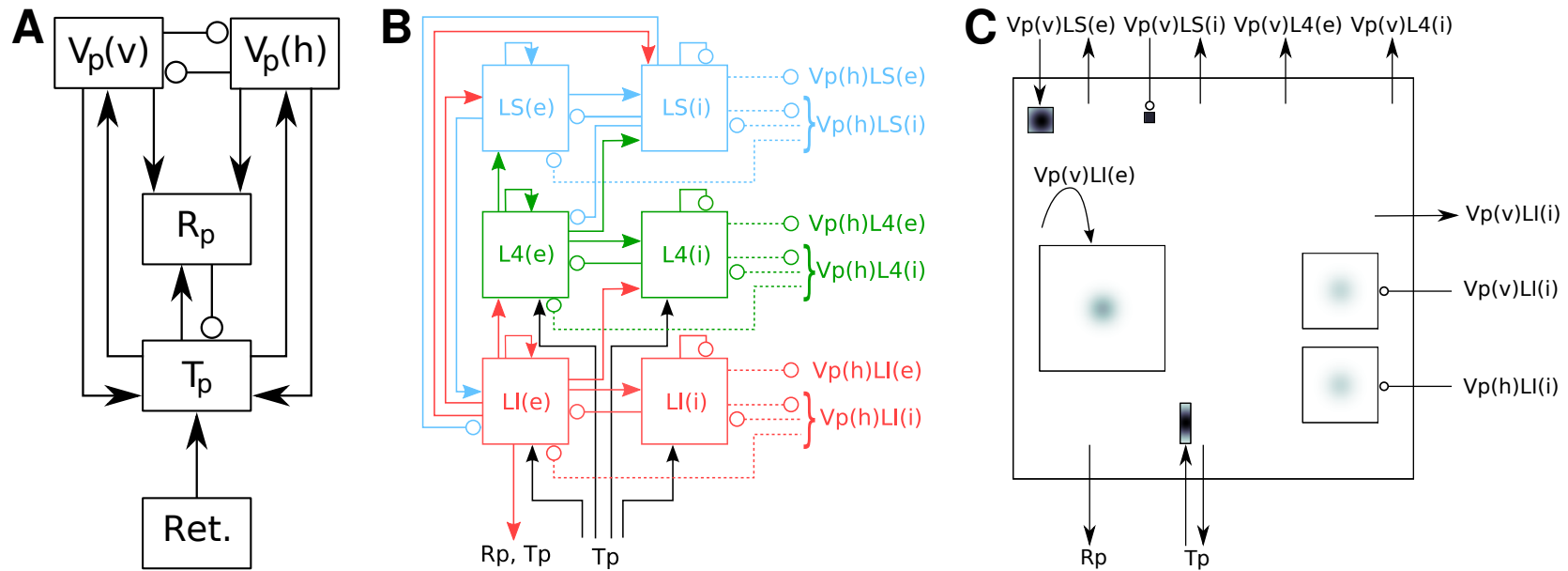
- ▶ graphically
- ▶ formally
- ▶ conceptually
- ▶ ontologically

Graphical representation:



Nordlie et al. Towards Reproducible Descriptions of Neuronal Network Models. PLoS Comput Biol 5(8): e1000456 (2009)

Graphical representation:



Nordlie et al. Towards Reproducible Descriptions of Neuronal Network Models. PLoS Comput Biol 5(8): e1000456 (2009)

Formal representation:

A Model Summary	
Populations	Eight: primary and secondary pathway, each comprising retina, thalamus (two layers), reticular nucleus, cortex (three layers)
Topology	Cartesian grids using visual-space coordinates
Connectivity	Random divergent connections described by probability kernels and cut-off masks
Neuron model	Leaky integrate-and-fire, fixed threshold, no absolute refractory time
Channel models	Slow hyperpolarizing channel
Synapse model	Conductance-based difference-of-exponentials (AMPA, GABA _A , GABA _B), additional instantaneous sigmoidal voltage dependence (NMDA)
Plasticity	—
Input	Thalamus: inhomogeneous Poisson spike trains reflecting drifting gratings; all neurons: spontaneous Poisson spike trains
Measurements	Membrane potential

Nordlie et al. Towards Reproducible Descriptions of Neuronal Network Models. PLoS Comput Biol 5(8): e1000456 (2009)

Formal representation:

C Topology	
Rectangular $8^\circ \times 8^\circ$ patch of parafoveal visual field mapped directly onto $N_p \times N_p$ and $N_s \times N_s$, respectively	
D Connectivity	
Type	Divergent connections drawn from a probabilistic kernels with cut-off masks, based on grid-distance
Kernel	$p(\vec{s}, \vec{t}) = p_0 e^{-\frac{ \vec{s}-\vec{t} }{\sigma}}$ (cf. [10, Tab. 3], p_0 : "Max pr. of connection", σ : "Space constant")
Mask	$p(\vec{s}, \vec{t}) = 0$ if $\begin{cases} s_x - t_x > \Delta_x/2 \text{ or} \\ s_y - t_y > \Delta_y/2 \end{cases}$ ($\Delta_{x,y}$: "arbor spread")
Weights	Fixed, identical for each synapse type, cf. [10, Tab. 1]
Delays	Fixed, drawn from Gaussian distribution with $\sigma = 1\text{ms}$, cut-off near 0ms implicit but not given in paper; for means see [10, p. 211, left column]

Nordlie et al. Towards Reproducible Descriptions of Neuronal Network Models. PLoS Comput Biol 5(8): e1000456 (2009)

Really formal representation: CSA

Connection Set Algebra by Mikael Djurfeldt

$$\begin{aligned}C &= \langle \bar{\rho}V, g, l \rangle \\V &= \phi(\sigma_d, c)d \\g &= g_dV + \rho N(0, \sigma_g, g_d) \\l &= r + d/v\end{aligned}$$

→ Mikael's talk

Conceptual representation:

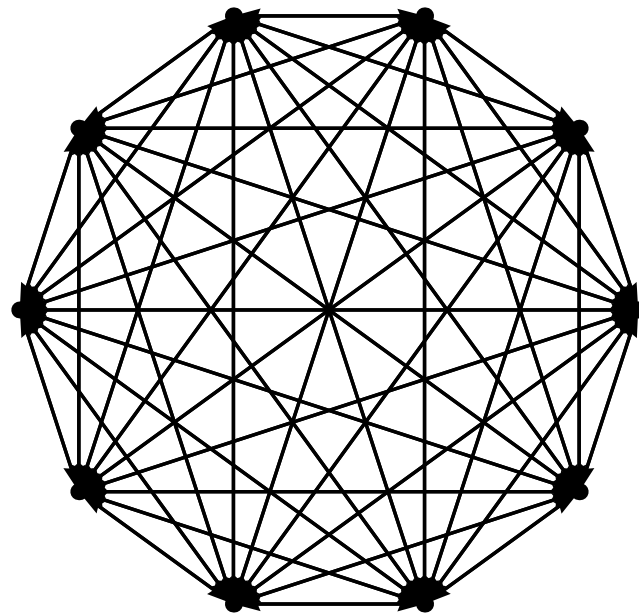
What do we mean by the terms we use to describe networks ?

Conceptual representation:

What do we mean by the terms we use to describe networks ?

- ▶ all-to-all

all-to-all:



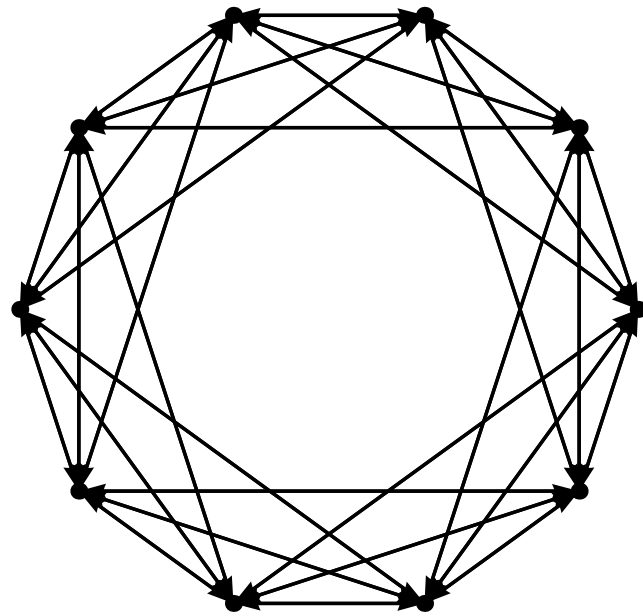
Conceptual representation:

What do we mean by the terms we use to describe networks ?

- ▶ all-to-all

- ▶ ring

ring:



Conceptual representation:

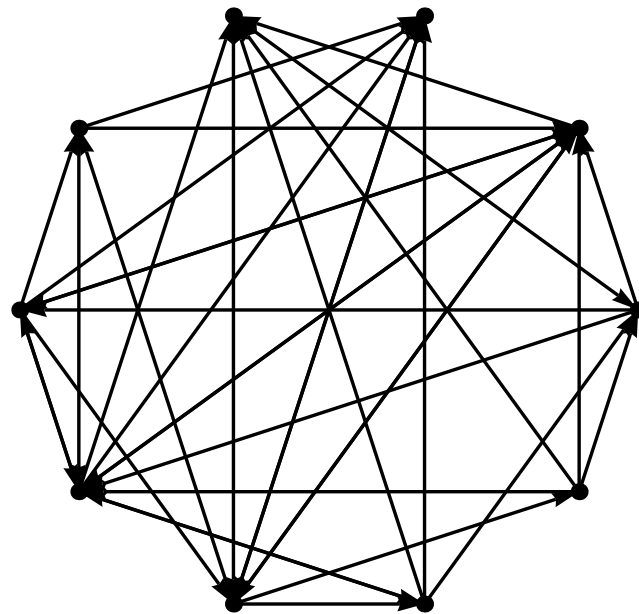
What do we mean by the terms we use to describe networks ?

- ▶ all-to-all

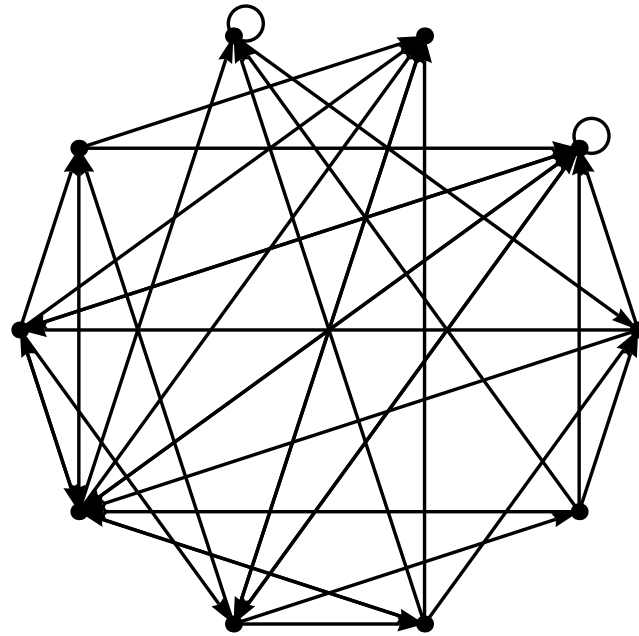
- ▶ ring

- ▶ random

random:



random:

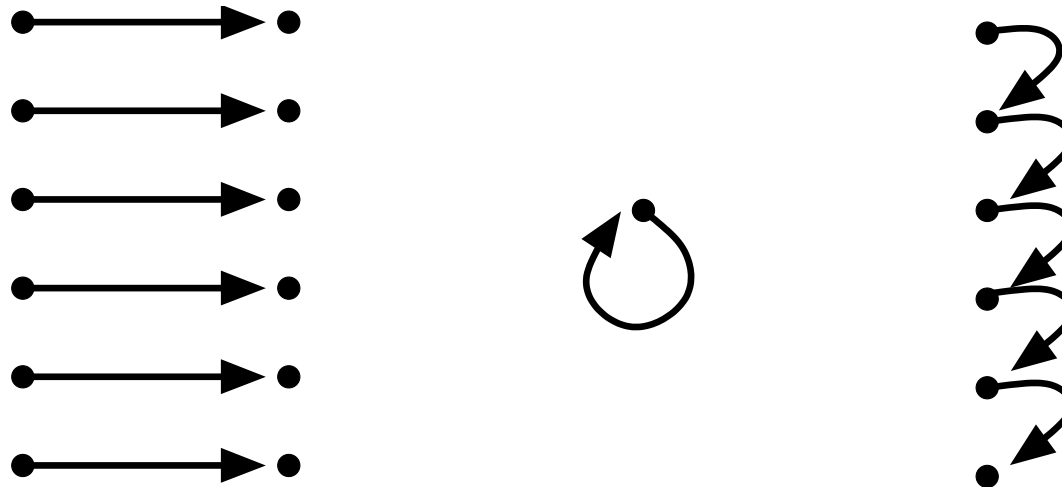


Conceptual representation:

What do we mean by the terms we use to describe networks?

- ▶ all-to-all
- ▶ ring
- ▶ random
- ▶ one-to-one?

one-to-one ?



→ Ontology, *CNO*, cf. Yann's talk

Workshop Sep 2011:

Creating, Documenting & Sharing Network Models

- ▶ started to set up a draft and plan a wiki on connectivity primitives (with Mikael Djurfeldt)
- ▶ try to systemize different terminologies used e. g. in NEST, CSA, PyNN, ... (e. g. RandomConvergentConnect vs. FanIn)
- ▶ hopefully allows for unambiguous network definitions

Some (subjective) ideas on connectivity primitives:

- ▶ work on sets of nodes and edges, i. e. *graphs*
- ▶ connectivity specifies which pairs of all possible pairs of nodes in a given set are connected by edges (aka adjacency/topology)
- ▶ connectivity primitives as 'minimal connectivity concepts'

Some (subjective) ideas on connectivity primitives:

- ▶ *connection primitive* is node-centric, i. e. defines connectivity between individual nodes
- ▶ *projection primitive* is edge-centric, i. e. defines connectivity between sets of nodes
- ▶ *graph primitive* is graph-centric, i. e. defines connectivity of entire graphs or ensembles

Some (subjective) ideas on connectivity primitives:

- ▶ connectivity primitives can be *local*, i. e. each node connects to other nodes independently of the state of the connectivity as a whole (i. e. the graph or any subset of it)
- ▶ *non-local* primitives are not independent of the connectivity of other nodes
- ▶ connectivity primitives can be *deterministic* or *probabilistic*

Possible examples for connection primitives (tbd):

- ▶ one-on-one-connection or edge (“synapse”)
- ▶ self-connection (“autapse”)
- ▶ one-to-many/many-to-one (“divergent/convergent”)
- ▶ multi-connection (“multapse”)
- ▶ random convergent/divergent (fan-in/fan-out): many-to-one/one-to-many + probability distribution

Possible examples for projection primitives (tbd):

- ▶ feed-forward all-to-all
- ▶ probabilistic (needs specification of distribution!)

Possible examples for graph primitives (tbd):

- ▶ Erdős-Rényi random graph
- ▶ Watts-and-Strogatz small world network

Values and attributes to specify connections:

▶ values:

- nodes can have position, membrane potential, preferred orientation, ...
- edges can have distance, weight, delay,...

▶ attributes:

- nodes can be “excitatory”, “parvalbumin expressing”, “compartment”, “synaptic contact point”, “LGN”, ...
- edges can be “static”, “plastic”, “current-based”, “AMPA”, ...

▶ establishment of connections can depend on all of these

Evaluation of probabilistic networks
– 2D spatial network example:

Embedding networks into a geometric space:

- ▶ connectivity will depend on
 - neuron distribution (uniform random, grid, non-uniform)
 - connectivity kernel (density or probability)
 - boundary conditions (open, periodic, mixture)

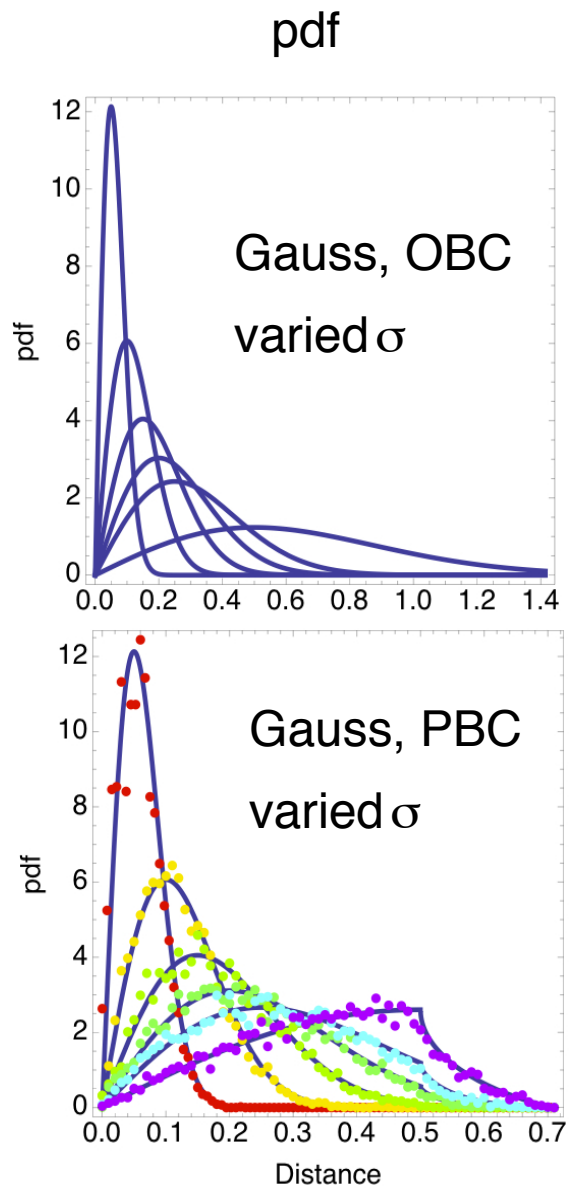
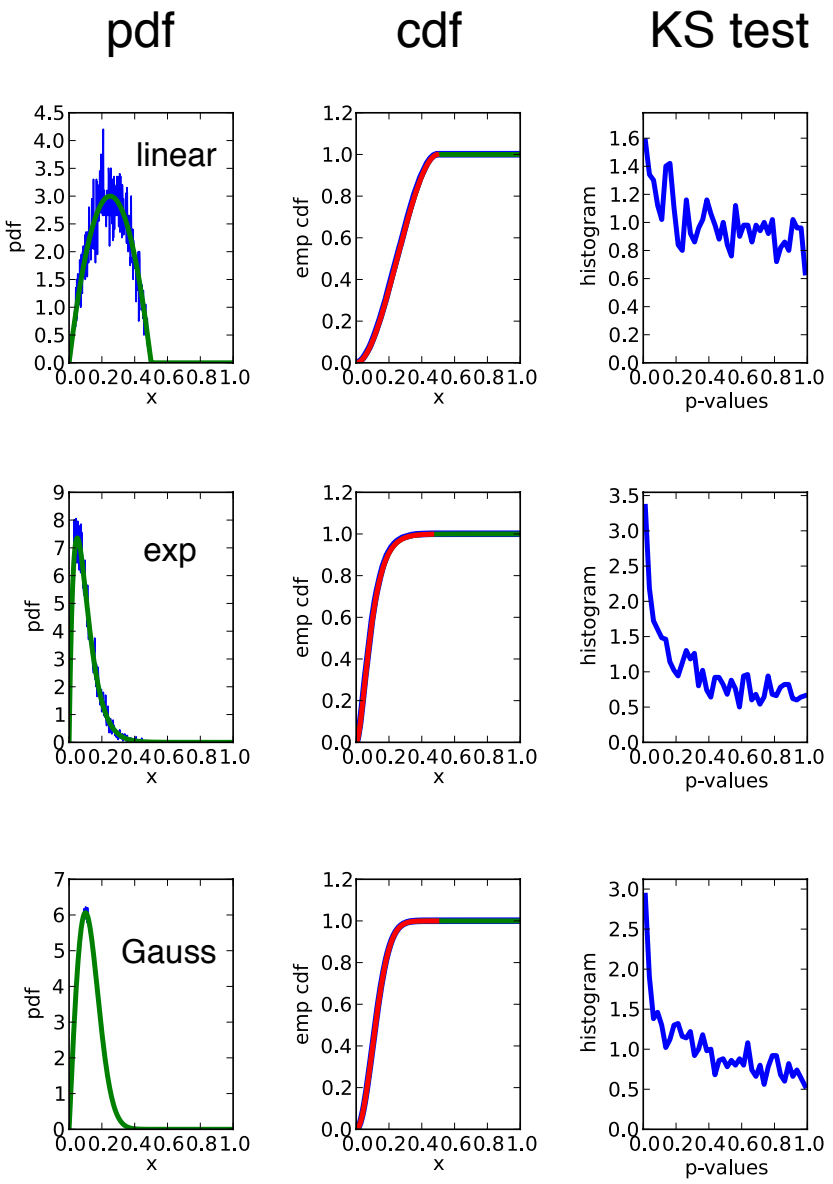
Embedding networks into a geometric space:

- ▶ connectivity will depend on
 - neuron distribution (uniform random, grid, non-uniform)
 - connectivity kernel (density or probability)
 - boundary conditions (open, periodic, mixture)
- ▶ analytical predictions of statistics of connectivity in dependence on these factors can be hard to achieve

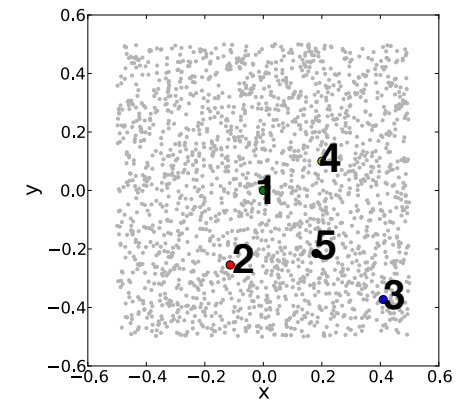
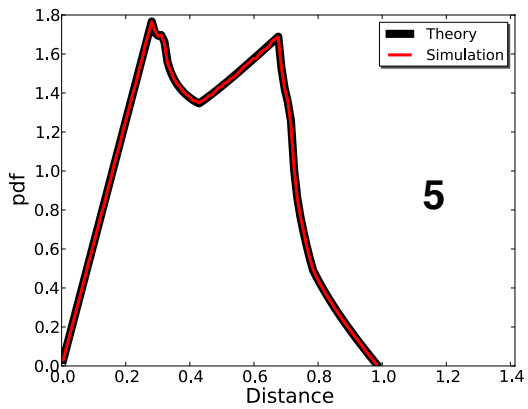
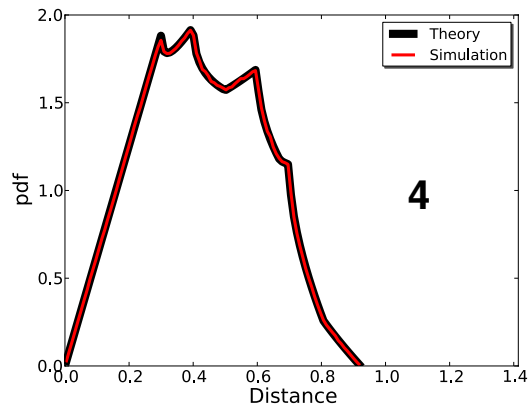
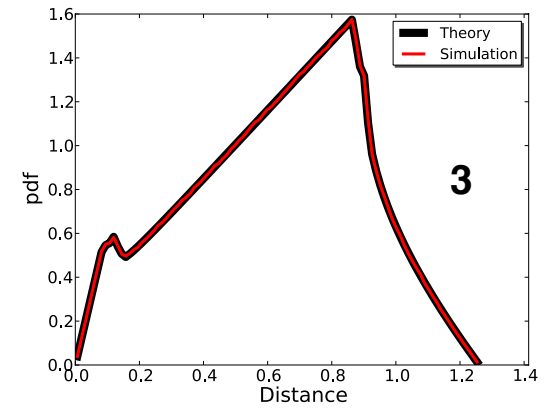
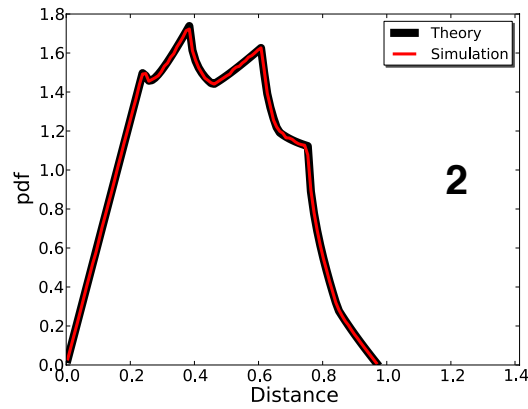
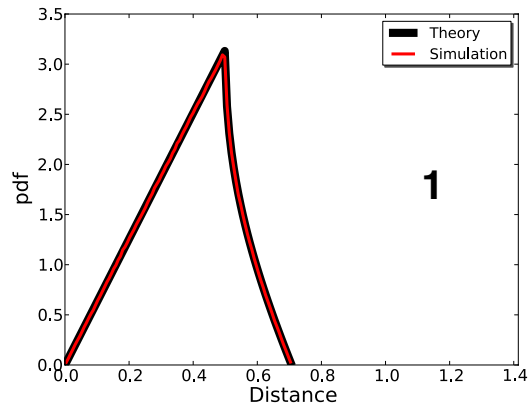
Embedding networks into a geometric space:

- ▶ connectivity will depend on
 - neuron distribution (uniform random, grid, non-uniform)
 - connectivity kernel (density or probability)
 - boundary conditions (open, periodic, mixture)
- ▶ analytical predictions of statistics of connectivity in dependence on these factors can be hard to achieve
- ▶ one of the most basic features: distribution of pairwise distances

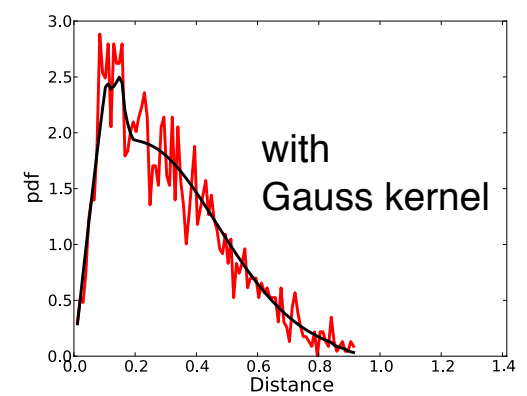
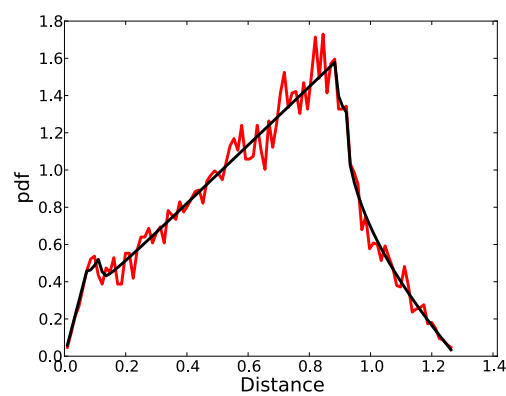
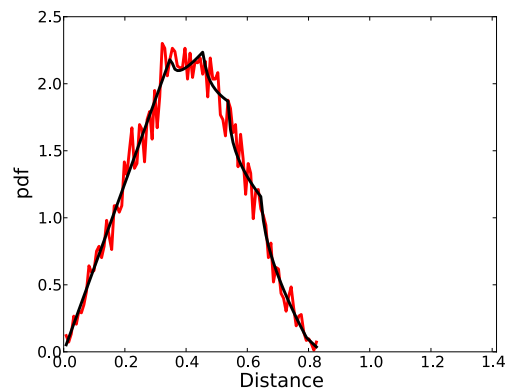
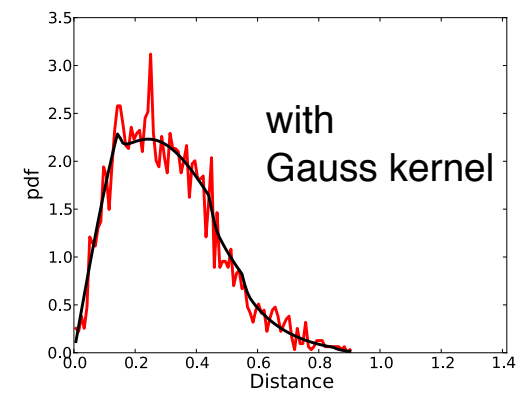
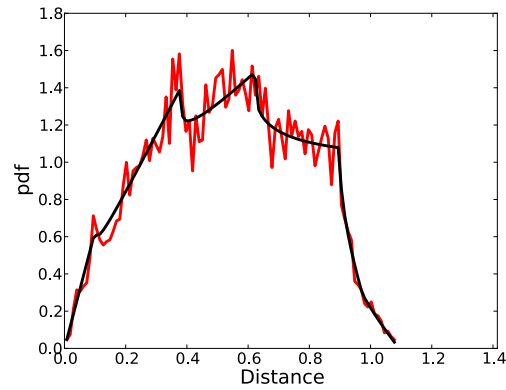
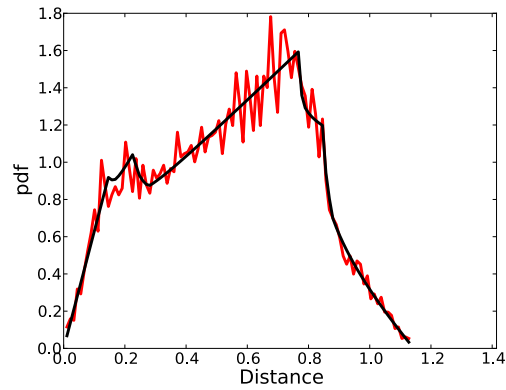
Periodic boundary conditions:



Open boundary conditions - position matters :



Finite sample size effects - the normal case:



Open questions:

Open questions:

- ▶ which degree of description detail suffices to specify a complex network?

Open questions:

- ▶ which degree of description detail suffices to specify a complex network?
- ▶ when can we be sure the simulator creates the networks we think it creates?

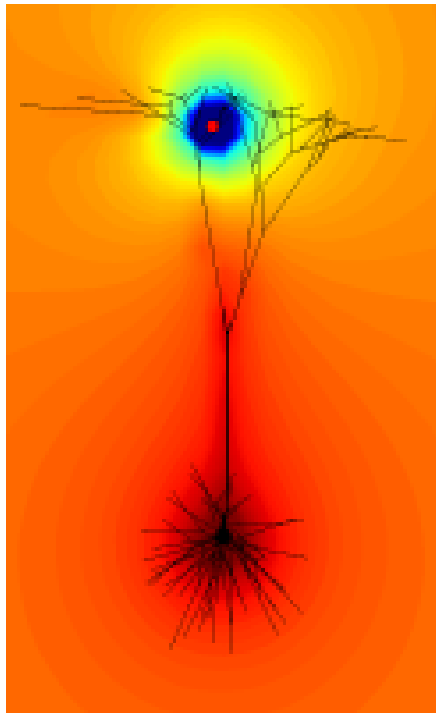
Open questions:

- ▶ which degree of description detail suffices to specify a complex network?
- ▶ when can we be sure the simulator creates the networks we think it creates?
- ▶ benchmark/common criteria for models used most often?

Open questions:

- ▶ which degree of description detail suffices to specify a complex network?
- ▶ when can we be sure the simulator creates the networks we think it creates?
- ▶ benchmark/common criteria for models used most often?
- ▶ how to deal with very large multi-population networks?
(cf. however Nordlie et al., PLoS Comput Biol 5(8):e10000456 (2009))

NEW !!!



LFPy

Local Field Potentials in Python

<http://compneuro.umb.no/LFPy/>

Thanks!